

Inspiring Futures  
Through Learning



**Exeter**  
a learning community

# Whole School Maths And Calculation Policy



Revised September 2020

P. Southwell



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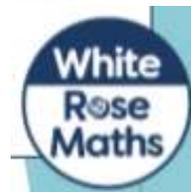
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# Inspiring Futures Through Learning

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## Mathematics at Exeter

Maths is an essential part of everyday life, as a child and an adult. We believe that high-quality maths teaching provides the firm foundations and roots for understanding the world, the ability to reason, problem-solve and promote a sense of enjoyment and curiosity about the subject, leading to successful, ambitious learners.

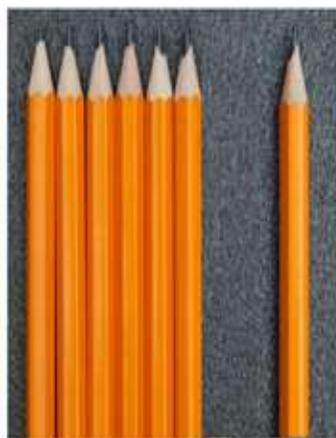
At Exeter a learning community we teach maths for mastery, an engaging and accessible style of mathematics teaching inspired by ; inspired and informed by the work of leading **maths** researchers and practitioners across the world. Our approach and aim is to develop a whole new culture of deep understanding, confidence and competence in **maths** – a culture that produces strong, secure learning and real progress that enhances mathematical understanding, enjoyment and achievement for every child. Children are encouraged to physically represent mathematical concepts. Objects and pictures are used to demonstrate and visualise abstract ideas, alongside numbers and symbols. Mathematical concepts are explored in a variety of representations and problem-solving contexts to give pupils a richer and deeper learning experience.

Our maths curriculum will promote:

- A secure understanding of the important concepts and an ability to make connections within mathematics.
- A broad range of skills in using and applying mathematics.
- An understanding of the importance of mathematical skills in everyday life.
- A fluent knowledge and recall of number facts and the number system.
- A commitment to and passion for mathematics
- The ability to show initiative and resilience in solving problems in a wide range of contexts, including the new or unusual.
- The ability to think independently and to persevere when faced with challenges, showing a confidence of success.
- The ability to embrace the value of learning from mistakes and false starts.
- The ability to reason, generalise and make sense of solutions.
- A wide range of mathematical vocabulary.

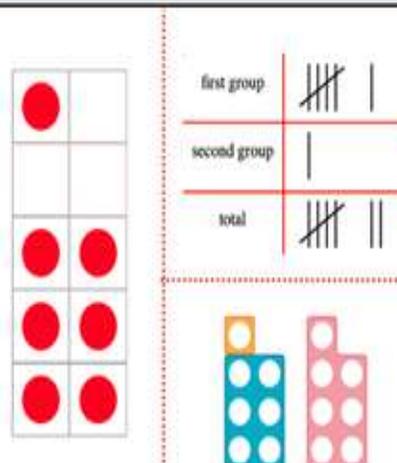
### Concrete

Using physical objects to help solve maths problems.



### Pictorial

Using a variety of drawings and models to solve maths problems and develop understanding.



### Abstract

Solve maths problems using only number and written methods.



## Expectations

<b>Books</b>	<p>Children should have a Mathematics book and an Arithmetic book. All <b>books</b> must be labelled with the subject, child's name and class. Books should be kept neat and presentable – one digit per square must be demonstrated when carrying out formal methods however when using some models and representations, this may not be possible.</p> <p>Pupil maths books should contain a daily <b>WALT and WILF</b>: there should be evidence of pupils' <b>varied fluency</b> linked to the learning objective; this should be represented by at least one appropriate model, different representations to show a deep level of understanding is desirable, learning should be backed up with the use of <b>concrete resources</b>. There should be evidence of pupils' application of this skill in a wider context with the use of <b>Reasoning and Problem solving</b> questions. Here mastery of the skills should be demonstrated by applying their learning, again a range of year-group specific models and representations is desirable. Books should be marked daily in accordance to the marking policy. Scaffolding should be used to support pupils who have not met the learning objective and questions can be posed to further develop the thinking of those who have achieved.</p>
<b>Fluency - Flashback slides</b>	<p><b>Fluency flashback</b> should be completed before every Maths lesson <u>in the back of Arithmetic books</u> - this is a quick 5 minute task where learning from the previous lesson, previous week, previous term and previous year are targeted. For most children it should be skills they are competent in, <b>it is not new learning</b>, questions are intended to reinforce the long term memory of pre-learnt skills. Questions can be used to consolidate skills from the previous unit where the WR unit tests identify a specific skill or type of question. These can be marked by the children.</p>
<b>Arithmetic</b>	<p><b>Arithmetic</b> should be completed daily – there should be enough questions to last 10 minutes (at roughly 30 seconds each) with an open-ended task or word problem to complete, for those who finish early. Questions should be able to be solved mentally by the higher ability children. Again this should <b>not be new learning</b> – questions should reinforce basic number skills and mental strategies. Questions should be mostly abstract and use the ARE formal method.</p>
<b>Working Walls</b>	<p><b>Math WW</b> to include: Key Q's, Sentence stems, Key Vocabulary, 100 square, Teacher Models (a focus on bar models) and must be up to date. Pupil work with positive comments or clarity of misconceptions is also desirable. Teacher models must be neat and presentable. They should be updated daily and be relevant to current learning.</p>
<b>Practical resources</b>	<p><b>Practical resources</b> should be labelled and available to use (<b>Covid- 19 precautions - limit cross contamination of resources -if central use, please wipe down and leave for 72hours before returning</b>) in all lessons, these should relate to the age related White Rose progression of skills.</p>
<b>Times Tables</b>	<p>Age related <b>Times tables</b> (up to 12x from Y3) must be visible, a larger focus display of one specific number needs to be changed every two weeks. A daily session of Fast Maths/TT Rock stars should be completed and recorded these are to be kept by all pupils their own file – an assessment 'number 3' should be completed at the end of each half term and updated on the school tracker to identify progress and intervention needs.</p>
<b>Display</b>	<p>Age related expectations display on (Autumn 2020 <b>shape and time</b>) a whole-school focus, based on Gap Analysis, should be clear and visible. It can be part of the Maths Working Wall or a separate display, it must be visible and informative. Use this to question children when lining up to maximise learning time</p>
<b>Every day math</b>	<p>Anything that can relate Maths to '<b>every day</b>' uses e.g.: By the sink – laminated measures of liquids, Round the clock – ARE vocabulary or questions Door frame – Measures in M/CM/MM conversion. Again these need to be a point of reference and questioning on a daily basis.</p>

Skill	Year	Representations and models
Add two 1-digit numbers to 10	1	Part-whole model Bar model Number shapes Ten frames (within 10) Bead strings (10) Number tracks
Add 1 and 2-digit numbers to 20	1	Part-whole model Bar model Number shapes Ten frames (within 20) Bead strings (20) Number tracks (labelled) Straws
Add three 1-digit numbers	2	Part-whole model Bar model Ten frames (within 20) Number shapes
Add 1 and 2-digit numbers to 100	2	Part-whole model Bar model Number lines (labelled) Number lines (blank) Straws Hundred square

# Addition

**Skill: Add 1-digit numbers within 10**      **Year: 1**

When adding numbers to 10, children can explore both aggregation and augmentation.

The part-whole model, discrete and continuous bar model, number shapes and ten frame support aggregation.

The combination bar model, ten frame, bead string and number track all support augmentation.

$4 + 3 = 7$

**Skill: Add 1 and 2-digit numbers to 20**      **Year: 1/2**

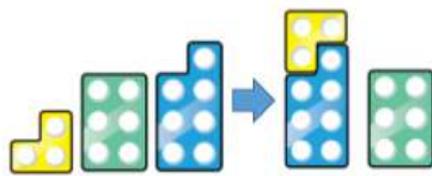
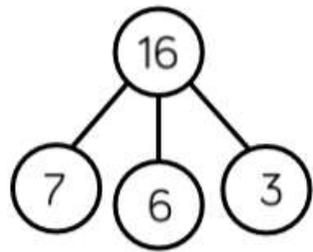
When adding one-digit numbers that cross 10, it is important to highlight the importance of ten ones equalling one ten.

Different manipulatives can be used to represent this exchange. Use concrete resources alongside number lines to support children in understanding how to partition their jumps.

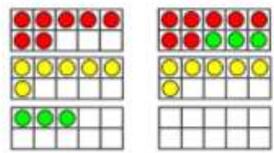
$8 + 7 = 15$

Skill: Add three 1-digit numbers

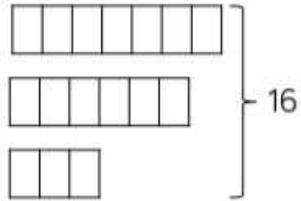
Year: 2



$$7 + 6 + 3 = 16$$



$$7 + 6 + 3 = 16$$



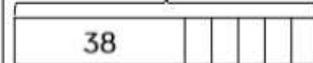
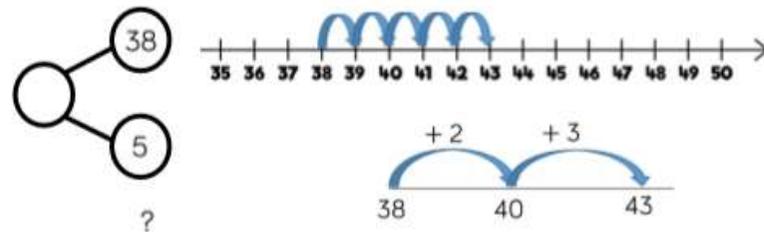
When adding three 1-digit numbers, children should be encouraged to look for number bonds to 10 or doubles to add the numbers more efficiently.

This supports children in their understanding of commutativity.

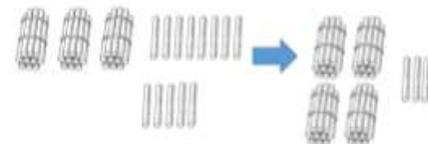
Manipulatives that highlight number bonds to 10 are effective when adding three 1-digit numbers.

Skill: Add 1-digit and 2-digit numbers to 100

Year: 2/3



$$38 + 5 = 43$$



1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100

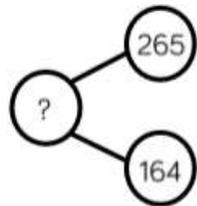
When adding single digits to a two-digit number, children should be encouraged to count on from the larger number.

They should also apply their knowledge of number bonds to add more efficiently e.g.  $8 + 5 = 13$  so  $38 + 5 = 43$ .

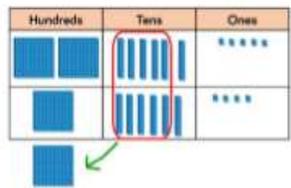
Hundred squares and straws can support children to find the number bond to 10.

Skill: Add numbers with up to 3 digits

Year: 3



$$265 + 164 = 429$$



$$\begin{array}{r} 265 \\ + 164 \\ \hline 429 \\ 1 \end{array}$$



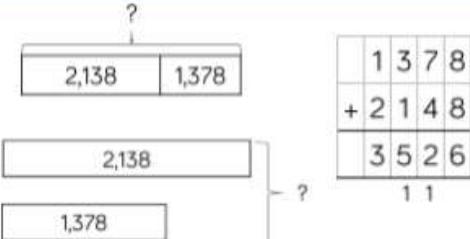
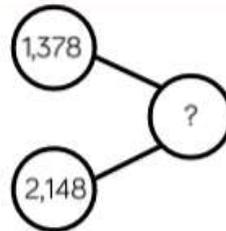
Base 10 and place value counters are the most effective manipulatives when adding numbers with up to 3 digits.

Ensure children write out their calculation alongside any concrete resources so they can see the links to the written column method.

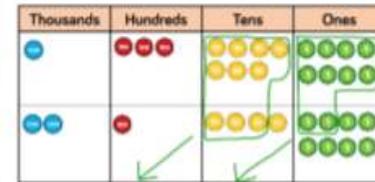
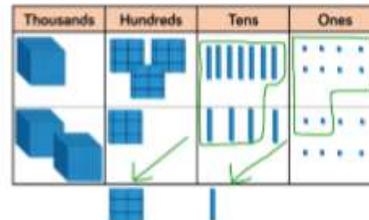
Plain counters on a place value grid can also be used to support learning.

Skill: Add numbers with up to 4 digits

Year: 4



$$1,378 + 2,148 = 3,526$$



Base 10 and place value counters are the most effective manipulatives when adding numbers with up to 4 digits.

Ensure children write out their calculation alongside any concrete resources so they can see the links to the written column method.

Plain counters on a place value grid can also be used to support learning.

Skill	Year	Representations and models
Add two 2-digit numbers	2	Part-whole model Bar model Number lines (blank) Straws Base 10 Place value counters Column addition
Add with up to 3-digits	3	Part-whole model Bar model Base 10 Place value counters Column addition
Add with up to 4-digits	4	Part-whole model Bar model Base 10 Place value counters Column addition
Add with more than 4 digits	5	Part-whole model Bar model Place value counters Column addition
Add with up to 3 decimal places	5	Part-whole model Bar model Place value counters Column addition

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## Addition

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**Skill: Add with up to 3 decimal places**      **Year: 5**

Diagram illustrating the addition of 2.41 and 3.65. It shows a part-whole model with 2.41 and 3.65 in circles, a bar model with 3.65 and 2.41, and a column addition showing the result 6.06. A box contains the equation  $3.65 + 2.41 = 6.06$ .

Place value counters and plain counters on a place value grid are the most effective manipulatives when adding decimals with 1, 2 and then 3 decimal places.

Ensure children have experience of adding decimals with a variety of decimal places. This includes putting this into context when adding money and other measures.

**Skill: Add numbers with more than 4 digits**      **Year: 5/6**

Diagram illustrating the addition of 104,328 and 61,731. It shows a part-whole model with 104,328 and 61,731 in circles, a bar model with 104,328 and 61,731, and a column addition showing the result 166,059. A box contains the equation  $104,328 + 61,731 = 166,059$ .

Place value counters or plain counters on a place value grid are the most effective concrete resources when adding numbers with more than 4 digits.

At this stage, children should be encouraged to work in the abstract, using the column method to add larger numbers efficiently.

Skill	Year	Representations and models
Subtract two 1-digit numbers to 10	1	Part-whole model Bar model Number shapes Ten frames (within 10) Bead strings (10) Number tracks
Subtract 1 and 2-digit numbers to 20	1	Part-whole model Bar model Number shapes Ten frames (within 20) Bead string (20) Number tracks Number lines (labelled) Straws
Subtract 1 and 2-digit numbers to 100	2	Part-whole model Bar model Number lines (labelled) Number lines (blank) Straws Hundred square
Subtract two 2-digit numbers	2	Part-whole model Bar model Number lines (blank) Straws Base 10 Place value counters Column addition

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## Subtraction

Skill: Subtract 1-digit numbers within 10	Year: 1
<p><math>7 - 3 = 4</math></p>	<p>Part-whole models, bar models, ten frames and number shapes support partitioning.</p> <p>Ten frames, number tracks, single bar models and bead strings support reduction.</p> <p>Cubes and bar models with two bars can support finding the difference.</p>

Skill: Subtract 1 and 2-digit numbers to 20	Year: 1/2
<p><math>14 - 6 = 8</math></p>	<p>When subtracting one-digit numbers that cross 10, it is important to highlight the importance of ten ones equalling one ten.</p> <p>Children should be encouraged to find the number bond to 10 when partitioning the subtracted number. Ten frames, number shapes and number lines are particularly useful for this.</p>

Skill	Year	Representations and models
Subtract with up to 3-digits	3	Part-whole model Bar model Base 10 Place value counters Column addition
Subtract with up to 4-digits	4	Part-whole model Bar model Base 10 Place value counters Column addition
Subtract with more than 4 digits	5	Part-whole model Bar model Place value counters Column addition
Subtract with up to 3 decimal places	5	Part-whole model Bar model Place value counters Column addition

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# Subtraction

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Skill: Subtract 1 and 2-digit numbers to 100	Year: 2						
<p>65</p> <p>28</p> <p>65</p> <p>?</p> <p>28</p> <p><math>65 - 28 = 37</math></p> <table border="1"> <thead> <tr> <th>Tens</th> <th>Ones</th> </tr> </thead> <tbody> <tr> <td> </td> <td> </td> </tr> <tr> <td> </td> <td> </td> </tr> </tbody> </table>	Tens	Ones					<p>At this stage, encourage children to use the formal column method when calculating alongside straws, base 10 or place value counters. As numbers become larger, straws become less efficient.</p> <p>Children can also use a blank number line to count on to find the difference. Encourage them to jump to multiples of 10 to become more efficient.</p>
Tens	Ones						

Skill: Subtract numbers with up to 3 digits	Year: 3						
<p>435</p> <p>273</p> <p>?</p> <p>435</p> <p>273</p> <p>?</p> <p><math>435 - 273 = 262</math></p> <table border="1"> <thead> <tr> <th>Hundreds</th> <th>Tens</th> <th>Ones</th> </tr> </thead> <tbody> <tr> <td> </td> <td> </td> <td> </td> </tr> </tbody> </table>	Hundreds	Tens	Ones				<p>Base 10 and place value counters are the most effective manipulative when subtracting numbers with up to 3 digits.</p> <p>Ensure children write out their calculation alongside any concrete resources so they can see the links to the written column method.</p> <p>Plain counters on a place value grid can also be used to support learning.</p>
Hundreds	Tens	Ones					

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### Skill: Subtract numbers with up to 4 digits

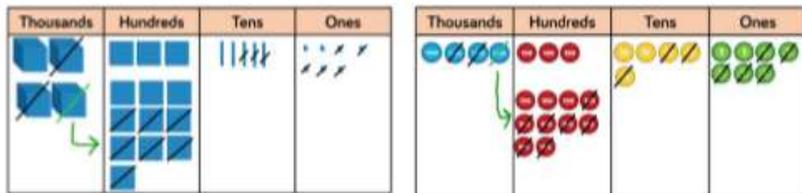
Year: 4

$4,357 - 2,735 = 1,622$

Base 10 and place value counters are the most effective manipulatives when subtracting numbers with up to 4 digits.

Ensure children write out their calculation alongside any concrete resources so they can see the links to the written column method.

Plain counters on a place value grid can also be used to support learning.



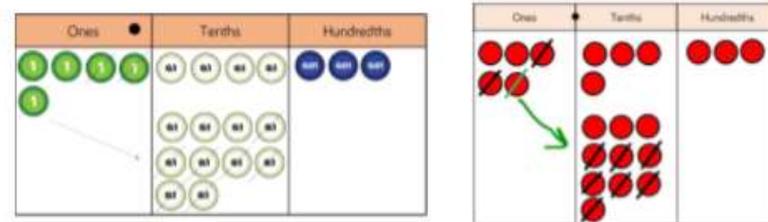
### Skill: Subtract with up to 3 decimal places

Year: 5

$5.43 - 2.7 = 2.73$

Place value counters and plain counters on a place value grid are the most effective manipulative when subtracting decimals with 1, 2 and then 3 decimal places.

Ensure children have experience of subtracting decimals with a variety of decimal places. This includes putting this into context when subtracting money and other measures.



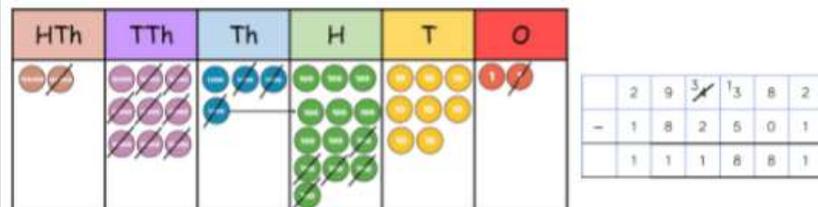
### Skill: Subtract numbers with more than 4 digits

Year: 5/6

$294,382 - 182,501 = 111,881$

Place value counters or plain counters on a place value grid are the most effective concrete resource when subtracting numbers with more than 4 digits.

At this stage, children should be encouraged to work in the abstract, using column method to subtract larger numbers efficiently.



## Glossary

**Addend** - A number to be added to another.

**Aggregation** - combining two or more quantities or measures to find a total.

**Augmentation** - increasing a quantity or measure by another quantity.

**Commutative** - numbers can be added in any order.

**Complement** - in addition, a number and its complement make a total e.g. 300 is the complement to 700 to make 1,000

**Difference** - the numerical difference between two numbers is found by comparing the quantity in each group.

**Exchange** - Change a number or expression for another of an equal value.

**Minuend** - A quantity or number from which another is subtracted.

**Partitioning** - Splitting a number into its component parts.

**Reduction** - Subtraction as take away.

**Subitise** - Instantly recognise the number of objects in a small group without needing to count.

**Subtrahend** - A number to be subtracted from another.

**Sum** - The result of an addition.

**Total** - The aggregate or the sum found by addition.

Skill	Year	Representations and models	
Solve one-step problems with multiplication	1/2	Bar model Number shapes Counters	Ten frames Bead strings Number lines
Multiply 2-digit by 1-digit numbers	3/4	Place value counters Base 10	Short written method Expanded written method
Multiply 3-digit by 1-digit numbers	4	Place value counters Base 10	Short written method
Multiply 4-digit by 1-digit numbers	5	Place value counters	Short written method

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# Multiplication

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**Skill: Solve 1-step problems using multiplication**      **Year: 1/2**

One bag holds 5 apples.  
How many apples do 4 bags hold?

Children represent multiplication as repeated addition in many different ways.

In Year 1, children use concrete and pictorial representations to solve problems. They are not expected to record multiplication formally.

In Year 2, children are introduced to the multiplication symbol.

$5 + 5 + 5 + 5 = 20$   
 $4 \times 5 = 20$   
 $5 \times 4 = 20$

**Skill: Multiply 2-digit numbers by 1-digit numbers**      **Year: 3/4**

Teachers may decide to first look at the expanded column method before moving on to the short multiplication method. The place value counters should be used to support the understanding of the method rather than supporting the multiplication, as children should use times table knowledge.

$34 \times 5 = 170$

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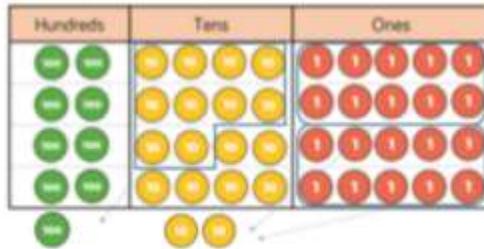
Skill: Multiply 3-digit numbers by 1-digit numbers

Year: 3/4



	H	T	O
	2	4	5
x			4
	9	8	0
	1	2	

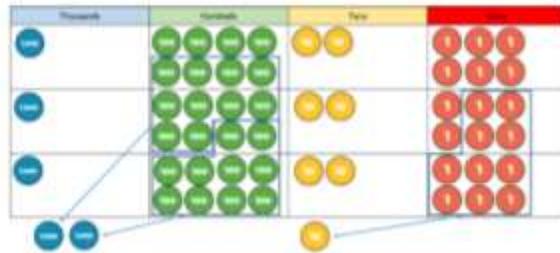
$$245 \times 4 = 980$$



When moving to 3-digit by 1-digit multiplication, encourage children to move towards the short, formal written method. Base 10 and place value counters continue to support the understanding of the written method. Limit the number of exchanges needed in the questions and move children away from resources when multiplying larger numbers.

Skill: Multiply 4-digit numbers by 1-digit numbers

Year: 5



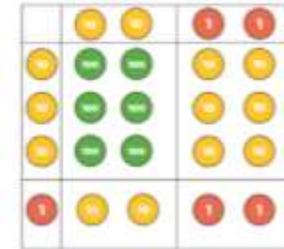
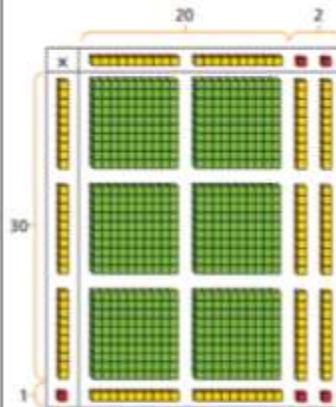
$$1,826 \times 3 = 5,478$$

	Th	H	T	O
	1	8	2	6
x				3
	5	4	7	8
	2	1		

When multiplying 4-digit numbers, place value counters are the best manipulative to use to support children in their understanding of the formal written method. If children are multiplying larger numbers and struggling with their times tables, encourage the use of multiplication grids so children can focus on the use of the written method.

Skill: Multiply 2-digit numbers by 2-digit numbers

Year: 5



x	20	2
30	600	60
1	20	2

	H	T	O
		2	2
x		3	1
	6	2	2
	6	8	0
	6	8	2

$$22 \times 31 = 682$$

When multiplying a multi-digit number by 2-digits, use the area model to help children understand the size of the numbers they are using. This links to finding the area of a rectangle by finding the space covered by the Base 10. The grid method matches the area model as an initial written method before moving on to the formal written multiplication method.

# Multiplication

Skill	Year	Representations and models
Multiply 2-digit by 2-digit numbers	5	Place value counters Base 10 Short written method Grid method
Multiply 2-digit by 3-digit numbers	5	Place value counters Short written method Grid method
Multiply 2-digit by 4-digit numbers	5/6	Formal written method

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# Multiplication

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Skill: Multiply 3-digit numbers by 2-digit numbers	Year: 5																														
 <table border="1" data-bbox="645 821 833 1109"> <thead> <tr> <th></th> <th>Th</th> <th>H</th> <th>T</th> <th>O</th> </tr> </thead> <tbody> <tr> <td></td> <td></td> <td>2</td> <td>3</td> <td>4</td> </tr> <tr> <td>x</td> <td></td> <td></td> <td>3</td> <td>2</td> </tr> <tr> <td></td> <td></td> <td>4</td> <td>6</td> <td>8</td> </tr> <tr> <td>1</td> <td>7</td> <td>1</td> <td>0</td> <td>2</td> </tr> <tr> <td>7</td> <td>4</td> <td>8</td> <td>8</td> <td></td> </tr> </tbody> </table>		Th	H	T	O			2	3	4	x			3	2			4	6	8	1	7	1	0	2	7	4	8	8		<p>Children can continue to use the area model when multiplying 3-digits by 2-digits. Place value counters become more efficient to use but Base 10 can be used to highlight the size of numbers.</p> <p>Encourage children to move towards the formal written method, seeing the links with the grid method.</p>
	Th	H	T	O																											
		2	3	4																											
x			3	2																											
		4	6	8																											
1	7	1	0	2																											
7	4	8	8																												
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x	200	30	4																												
30	6,000	900	120																												
2	400	60	8																												
<div style="border: 1px solid black; padding: 5px; display: inline-block;"> <math>234 \times 32 = 7,488</math> </div>																															

Skill: Multiply 4-digit numbers by 2-digit numbers	Year: 5/6																																																	
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	TTh	Th	H	T	O																																													
		2	7	3	9																																													
x				2	8																																													
				4	6																																													
2	1	9	1	2																																														
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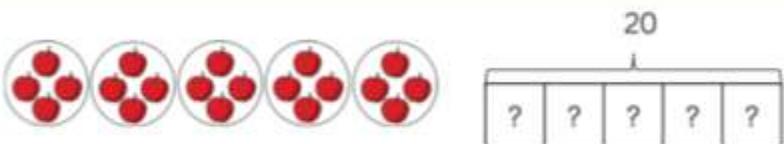
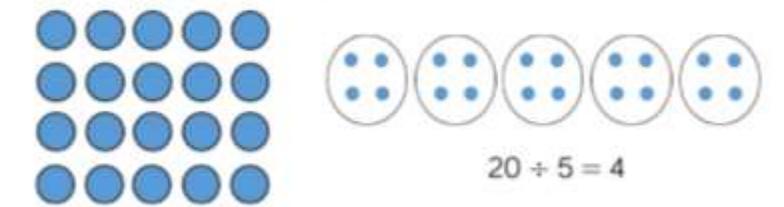
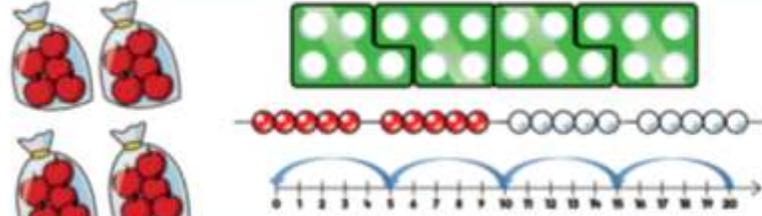
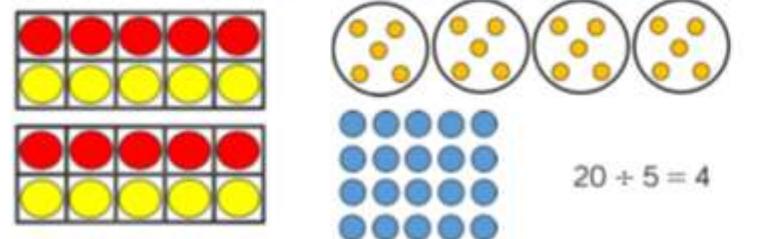
xeter

Skill	Year	Representations and models
Solve one-step problems with division (sharing)	1/2	Bar model Real life objects Arrays Counters
Solve one-step problems with division (grouping)	1/2	Real life objects Number shapes Bead strings Ten frames Number lines Arrays Counters
Divide 2-digits by 1-digit (no exchange sharing)	3	Straws Base 10 Bar model Place value counters Part-whole model
Divide 2-digits by 1-digit (sharing with exchange)	3	Straws Base 10 Bar model Place value counters Part-whole model

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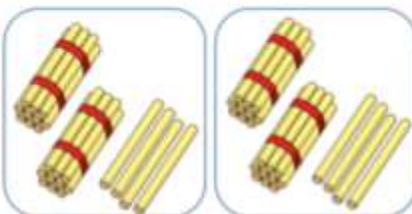
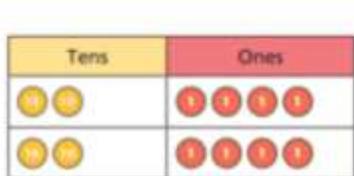
## Division

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Skill: Solve 1-step problems using multiplication (sharing)	Year: 1/2	Skill: Solve 1-step problems using division (grouping)	Year: 1/2
 <p>There are 20 apples altogether. They are shared equally between 5 bags. How many apples are in each bag?</p>  <p><math>20 \div 5 = 4</math></p>	<p>Children solve problems by sharing amounts into equal groups.</p> <p>In Year 1, children use concrete and pictorial representations to solve problems. They are not expected to record division formally.</p> <p>In Year 2, children are introduced to the division symbol.</p>	 <p>There are 20 apples altogether. They are put in bags of 5. How many bags are there?</p>  <p><math>20 \div 5 = 4</math></p>	<p>Children solve problems by grouping and counting the number of groups. Grouping encourages children to count in multiples and links to repeated subtraction on a number line. They can use concrete representations in fixed groups such as number shapes which helps to show the link between multiplication and division.</p>

**Skill: Divide 2-digits by 1-digit (sharing with no exchange)**

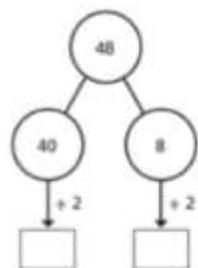
**Year: 1/2**



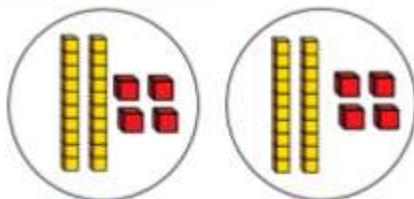
When dividing larger numbers, children can use manipulatives that allow them to partition into tens and ones.

Straws, Base 10 and place value counters can all be used to share numbers into equal groups.

Part-whole models can provide children with a clear written method that matches the concrete representation.

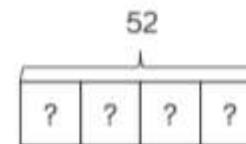
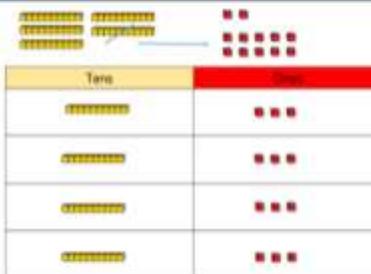


$$48 \div 2 = 24$$

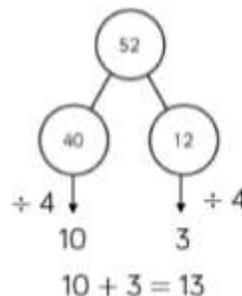


**Skill: Divide 2-digits by 1-digit (sharing with exchange)**

**Year: 3/4**



$$52 \div 4 = 13$$



When dividing numbers involving an exchange, children can use Base 10 and place value counters to exchange one ten for ten ones.

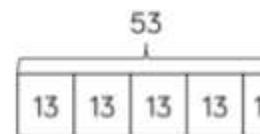
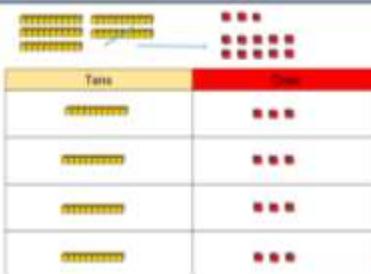
Children should start with the equipment outside the place value grid before sharing the tens and ones equally between the rows.

Flexible partitioning in a part-whole model supports this method.

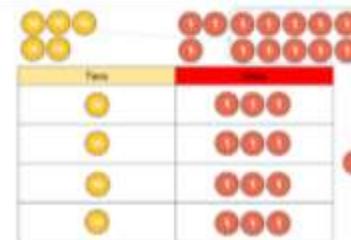
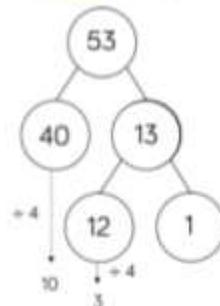
Skill	Year	Representations and models	
Divide 2-digits by 1-digit (sharing with remainders)	3/4	Straws Base 10 Bar model	Place value counters Part-whole model
Divide 2-digits by 1-digit (grouping)	4/5	Place value counters Counters	Place value grid Written short division
Divide 3-digits by 1-digit (sharing with exchange)	4	Base 10 Bar model	Place value counters Part-whole model
Divide 3-digits by 1-digit (grouping)	4/5	Place value counters Counters	Place value grid Written short division

**Skill: Divide 2-digits by 1-digit (sharing with remainders)**

**Year: 3/4**



$$52 \div 4 = 13 \text{ r}1$$



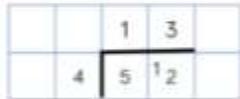
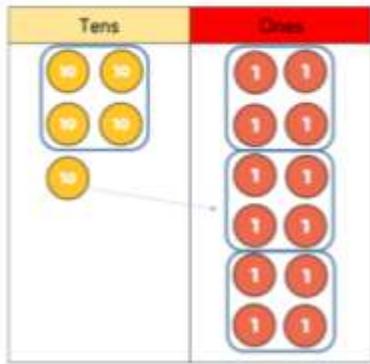
When dividing numbers with remainders, children can use Base 10 and place value counters to exchange one ten for ten ones.

Starting with the equipment outside the place value grid will highlight remainders, as they will be left outside the grid once the equal groups have been made.

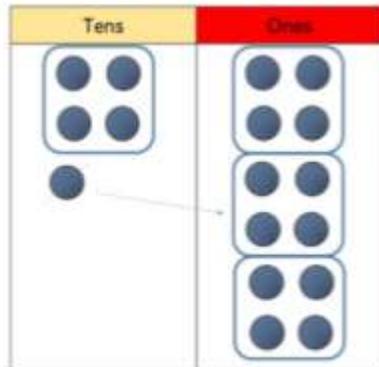
Flexible partitioning in a part-whole model supports this method.

Skill: Divide 2-digits by 1-digit (grouping)

Year: 4/5



$$52 \div 4 = 13$$



When using the short division method, children use grouping. Starting with the largest place value, they group by the divisor.

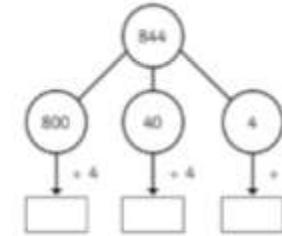
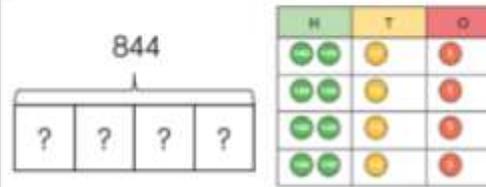
Language is important here. Children should consider 'How many groups of 4 tens can we make?' and 'How many groups of 4 ones can we make?'

Remainders can also be seen as they are left ungrouped.

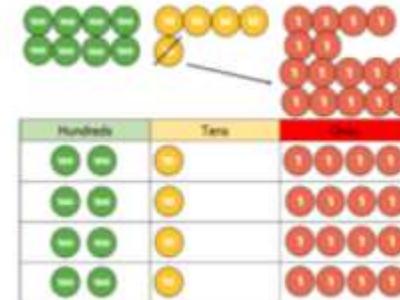
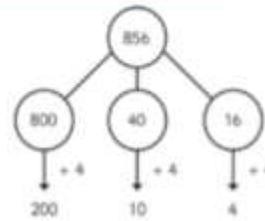
Skill: Divide 3-digits by 1-digit (sharing)

Year: 4

$$844 \div 4 = 122$$



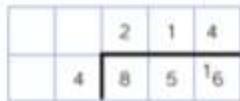
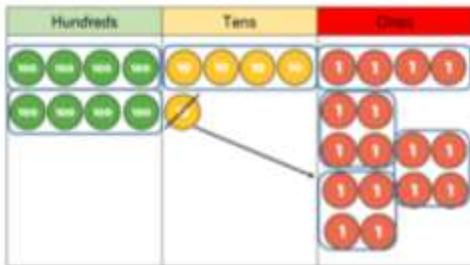
$$844 \div 4 = 122$$



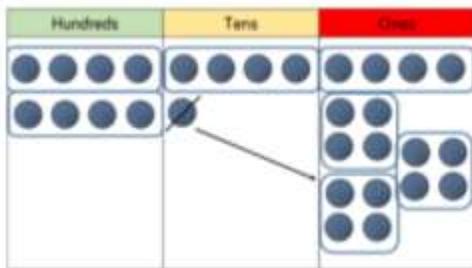
Children can continue to use place value counters to share 3-digit numbers into equal groups. Children should start with the equipment outside the place value grid before sharing the hundreds, tens and ones equally between the rows. This method can also help to highlight remainders. Flexible partitioning in a part-whole model supports this method.

Skill: Divide 3-digits by 1-digit (grouping)

Year: 5



$$856 \div 4 = 214$$



Children can continue to use grouping to support their understanding of short division when dividing a 3-digit number by a 1-digit number.

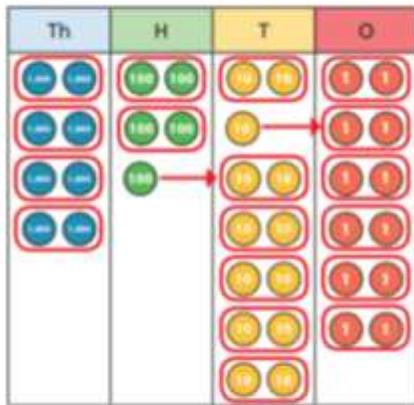
Place value counters or plain counters can be used on a place value grid to support this understanding. Children can also draw their own counters and group them through a more pictorial method.

# Division

Skill	Year	Representations and models	
Divide 4-digits by 1-digit (grouping)	5	Place value counters Counters	Place value grid Written short division
Divide multi-digits by 2-digits (short division)	6	Written short division	List of multiples
Divide multi-digits by 2-digits (long division)	6	Written long division	List of multiples

**Skill: Divide 4-digits by 1-digit (grouping)**

**Year: 5**



	4	2	6	6
2	8	5	13	12

Place value counters or plain counters can be used on a place value grid to support children to divide 4-digits by 1-digit. Children can also draw their own counters and group them through a more pictorial method.

Children should be encouraged to move away from the concrete and pictorial when dividing numbers with multiple exchanges.

$$8,532 \div 2 = 4,266$$

# Division

**Skill: Divide multi digits by 2-digits (short division)**

**Year: 6**

		0	3	6
12	4	4	3	7 2

$$432 \div 12 = 36$$

When children begin to divide up to 4-digits by 2-digits, written methods become the most accurate as concrete and pictorial representations become less effective. Children can write out multiples to support their calculations with larger remainders. Children will also solve problems with remainders where the quotient can be rounded as appropriate.

$$7,335 \div 15 = 489$$

		0	4	8	9
15	7	7 3	13 3	13 5	

15	30	45	60	75	90	105	120	135	150
----	----	----	----	----	----	-----	-----	-----	-----

**Skill: Divide multi-digits by 2-digits (long division)**

**Year: 6**

		0	3	6
12	4	3	2	
-	3	6	0	
		7	2	
-		7	2	
			0	

(x30)  
(x6)

$$432 \div 12 = 36$$

$$7,335 \div 15 = 489$$

		0	4	8	9
15	7	3	3	5	
-	6	0	0	0	
		1	3	3	5
-		1	2	0	0
			1	3	5
-			1	3	5
				0	

(x400)  
(x80)  
(x9)

- 1 x 15 = 15
- 2 x 15 = 30
- 3 x 15 = 45
- 4 x 15 = 60
- 5 x 15 = 75
- 10 x 15 = 150

Children can also divide by 2-digit numbers using long division.

Children can write out multiples to support their calculations with larger remainders.

Children will also solve problems with remainders where the quotient can be rounded as appropriate.

$$372 \div 15 = 24 \text{ r}12$$

			2	4	r	1	2
1	5	3	7	2			
		-	3	0	0		
				7	2		
		-		6	0		
				1	2		

$1 \times 15 = 15$   
 $2 \times 15 = 30$   
 $3 \times 15 = 45$   
 $4 \times 15 = 60$   
 $5 \times 15 = 75$   
 $10 \times 15 = 150$

When a remainder is left at the end of a calculation, children can either leave it as a remainder or convert it to a fraction. This will depend on the context of the question.

Children can also answer questions where the quotient needs to be rounded according to the context.

			2	4	$\frac{4}{5}$
1	5	3	7	2	
		-	3	0	0
				7	2
		-		6	0
				1	2

$$372 \div 15 = 24 \frac{4}{5}$$

## Division

## Glossary

**Array** – An ordered collection of counters, cubes or other item in rows and columns.

**Commutative** – Numbers can be multiplied in any order.

**Dividend** – In division, the number that is divided.

**Divisor** – In division, the number by which another is divided.

**Exchange** – Change a number or expression for another of an equal value.

**Factor** – A number that multiplies with another to make a product.

**Multiplicand** – In multiplication, a number to be multiplied by another.

**Partitioning** – Splitting a number into its component parts.

**Product** – The result of multiplying one number by another.

**Quotient** – The result of a division

**Remainder** – The amount left over after a division when the divisor is not a factor of the dividend.

**Scaling** – Enlarging or reducing a number by a given amount, called the scale factor

# Times Tables

Skill	Year	Representations and models
Recall and use multiplication and division facts for the 2-times table	2	Bar model Number shapes Counters Money Ten frames Bead strings Number lines Everyday objects
Recall and use multiplication and division facts for the 5-times table	2	Bar model Number shapes Counters Money Ten frames Bead strings Number lines Everyday objects
Recall and use multiplication and division facts for the 10-times table	2	Hundred square Number shapes Counters Money Ten frames Bead strings Number lines Base 10

**Skill: 2 times table** **Year: 2**

Encourage daily counting in multiples both forwards and backwards. This can be supported using a number line or a hundred square.

Look for patterns in the two times table, using concrete manipulatives to support. Notice how all the numbers are even and there is a pattern in the ones.

Use different models to develop fluency.

**Skill: 5 times table** **Year: 2**

Encourage daily counting in multiples both forwards and backwards. This can be supported using a number line or a hundred square.

Look for patterns in the five times table, using concrete manipulatives to support. Notice the pattern in the ones as well as highlighting the odd, even, odd, even pattern.

**Skill: 10 times table** **Year: 2**

Encourage daily counting in multiples both forwards and backwards. This can be supported using a number line or a hundred square.

Look for patterns in the ten times table, using concrete manipulatives to support. Notice the pattern in the digits- the ones are always 0, and the tens increase by 1 ten each time.

Skill	Year	Representations and models
Recall and use multiplication and division facts for the 3-times table	3	Hundred square Number shapes Counters Bead strings Number lines Everyday objects
Recall and use multiplication and division facts for the 4-times table	3	Hundred square Number shapes Counters Bead strings Number lines Everyday objects
Recall and use multiplication and division facts for the 8-times table	3	Hundred square Number shapes Bead strings Number tracks Everyday objects
Recall and use multiplication and division facts for the 6-times table	4	Hundred square Number shapes Bead strings Number tracks Everyday objects

**Skill: 3 times table** **Year: 3**

Encourage daily counting in multiples both forwards and backwards. This can be supported using a number line or a hundred square.

Look for patterns in the three times table, using concrete manipulatives to support. Notice the odd, even, odd, even pattern using number shapes to support. Highlight the pattern in the ones using a hundred square.

**Skill: 4 times table** **Year: 3**

Encourage daily counting in multiples, supported by a number line or a hundred square. Look for patterns in the four times table, using manipulatives to support. Make links to the 2 times table, seeing how each multiple is double the two. Notice the pattern in the ones within each group of five multiples. Highlight that all the multiples are even using number shapes to support.

**Skill: 8 times table** **Year: 3**

Encourage daily counting in multiples, supported by a number line or a hundred square. Look for patterns in the eight times table, using manipulatives to support. Make links to the 4 times table, seeing how each multiple is double the four. Notice the pattern in the ones within each group of five multiples. Highlight that all the multiples are even using number shapes to support.

### Skill: 6 times table

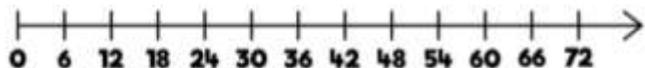
Year: 4



1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100



6	12	18	24	30
36	42	48	54	60
66	72	78	84	90



Encourage daily counting in multiples, supported by a number line or a hundred square. Look for patterns in the six times table, using manipulatives to support. Make links to the 3 times table, seeing how each multiple is double the three. Notice the pattern in the ones within each group of five multiples. Highlight that all the multiples are even using number shapes to support.

### Skill

Year

### Representations and models

Recall and use multiplication and division facts for the 7-times table

4

Hundred square  
Number shapes

Bead strings  
Number lines

Recall and use multiplication and division facts for the 9-times table

4

Hundred square  
Number shapes

Bead strings  
Number lines

Recall and use multiplication and division facts for the 11-times table

4

Hundred square  
Base 10

Place value counters  
Number lines

Recall and use multiplication and division facts for the 12-times table

4

Hundred square  
Base 10

Place value counters  
Number lines

### Skill: 7 times table

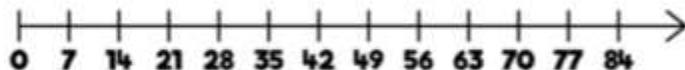
Year: 4



1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100

7	14	21	28	35
42	49	56	63	70

Encourage daily counting in multiples both forwards and backwards, supported by a number line or a hundred square. The seven times table can be trickier to learn due to the lack of obvious pattern in the numbers, however they already know several facts due to commutativity. Children can still see the odd, even pattern in the multiples using number shapes to support.



### Skill: 11 times table

Year: 4

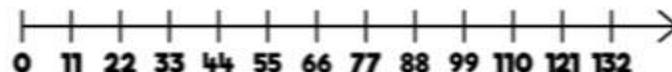
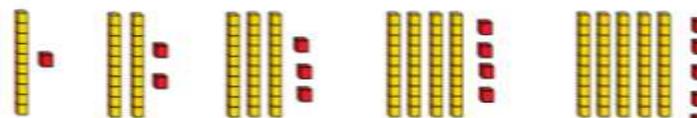
11	22	33	44	55	66
77	88	99	110	121	132

1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100



Encourage daily counting in multiples both forwards and backwards. This can be supported using a number line or a hundred square.

Look for patterns in the eleven times table, using concrete manipulatives to support. Notice the pattern in the tens and ones using the hundred square to support. Also consider the pattern after crossing 100



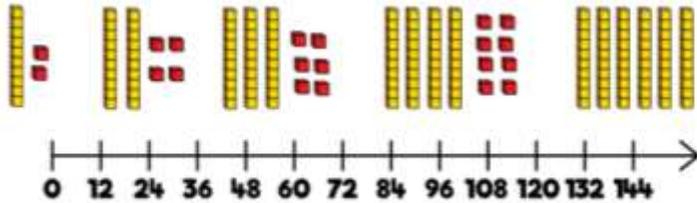
### Skill: 12 times table

Year: 4

12	24	36	48	60
72	84	96	108	120
132	144			

1	2	3	4	5	6	7	8	9	10
11	22	33	44	55	66	77	88	99	100
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100

Encourage daily counting in multiples, supported by a number line or a hundred square. Look for patterns in the 12 times table, using manipulatives to support. Make links to the 6 times table, seeing how each multiple is double the sixes. Notice the pattern in the ones within each group of five multiples. The hundred square can support in highlighting this pattern.



### Fast Maths 2020-21

#### Aims of Fast Maths

That children are confident learners who can recall every addition and multiplication fact within a second of being asked. Children who can do this will be successful in their Year 4 Times Tables test and Year 6 SATs.

Fast Maths should take 15 minutes maximum, 4 days a week. There is a two-week cycle, week 1 – A, week 2 – B.

1. Each child has 10 minutes to complete their fast maths grid (10x10 or 12x12).
2. The teacher then reads through each row of answers, the child using a diagonal line for each correct answer. If the answer is incorrect, leave unmarked.
3. The child writes in the time they completed the test in (if less than the 10 minutes allowed), how many errors they got (how many wrong answers, not now many left blank) and the correct number of answers.
4. This is transferred to their recording sheet.

Before starting Fast Maths, then the last week of each half term, children complete the Assertive Mentoring timetable test 3. This score is recorded and use for monitoring progress.



A more focussed times table approach can be taken when a specific times table are taught and consolidated by children – when children are confident with the tables up to 10 x 10 they should carry out Fast Maths.

